

Bonneville Adult Collection & Monitoring Facility (AFF) Hydraulic Design Calculations

CENWP-EC-HD

Comp by

SJS

12/21/12

Checked by

Hydraulic Data Collection Oct 31, 2012

Elevations (NGVD): Ref: BDF-2 -18/9 and BDF-2--18/24

Lower Exit Channel Invert (grating) =	39 ft, NGVD
Upper Exit Channel Invert (concr.) =	42 ft, NGVD
Floor supporting Valve 15, 14	32 ft, NGVD
Work Platform Floor =	45 ft, NGVD
Grating Platform (about 1.5" higher) =	45.1 ft, NGVD

Valve Pipe OD (field checked)

Valve 14	36 in =	3.0 feet
Valve 15	30 in =	2.5 feet
CL Valve Elevations		
Valve 14		33.5 ft, NGVD
Valve 15 (Z-15)		33.25 ft, NGVD

Main Exit Channel at Trashrack

Flow depth =	4.9 ft	WS Elev =	43.9 ft
Width =	8 ft		

Current Valve Settings:

Valve No.	14	15
% Open	0	75%

Weir Data

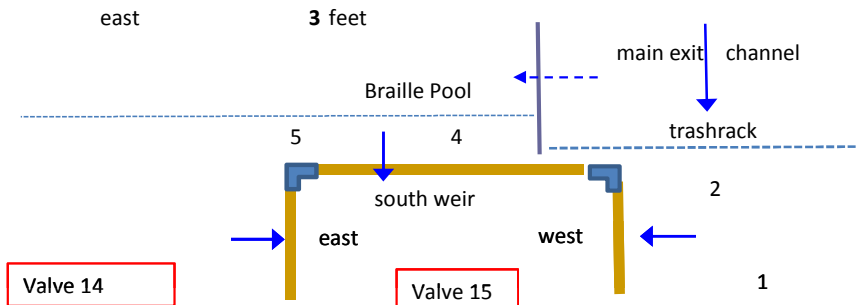
Distance from Top of Grating =	24.5 inches =	2.04 feet
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Weir

Elev =	43.04 ft
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Weir Lengths (open length between guides)

west	3 feet
south	6.5 feet
east	3 feet



Velocities Measured using Price Metter (single count setting)

Depth below WS (ft)	Lateral Location (looking U/s) in feet (Bi)					Integrated Average	Straight Average
	1	2.5	4	5.5	7		
0.5	2.85	3.31	3.44	2.60	2.06	2.81	2.85
1.5	3.15	3.12	2.20	1.81	1.89	2.44	2.44
2.5	2.00	2.04	1.01	1.32	1.41	1.57	1.56
3.5	1.37	0.76	0.68	0.60	0.96	0.91	0.87
4.3	0.64	0.51	0.62	0.49	0.90	0.65	0.63

Average Velocity (feet/sec) =	Integrated	Straight
	1.69	1.67
Computed Flow Rate (cfs) =	66.1	65.4

Integrated row average $V_j = \sum (B_{i+1} - B_i) * (V_i + V_{i+1})/2$ for $i = 0$ to n

$$V_0 = V_1 + (V_2 - V_1)/(B_2 - B_1) * (B_1 - B_0) * \text{Edge coef}$$

$$V_n = V_{n-1} + (V_{n-2} - V_{n-1})/(B_{n-2} - B_{n-1}) * (B_n - B_{n-1}) * \text{Edge coef}$$

Total Integrated average $V = \sum (Y_{j+1} - Y_j) * (V_j + V_{j+1})/2$ for $j = 0$ to n

$$V_0 = V_1 \quad \text{Surface same as 0.5 ft down}$$

$$V_n = V_{n-1} + (V_{n-2} - V_{n-1})/(Y_{n-2} - Y_{n-1}) * (Y_n - Y_{n-1}) * \text{Edge coef}$$

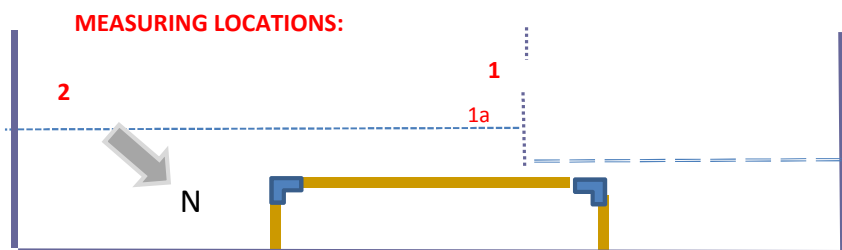
$$\text{Edge coeff} = 0.5$$

$$B_n = \text{total width}$$

$$Y_n = \text{m total depth}$$

Braille Pools Data

Depth of Pool at North end = 4 feet

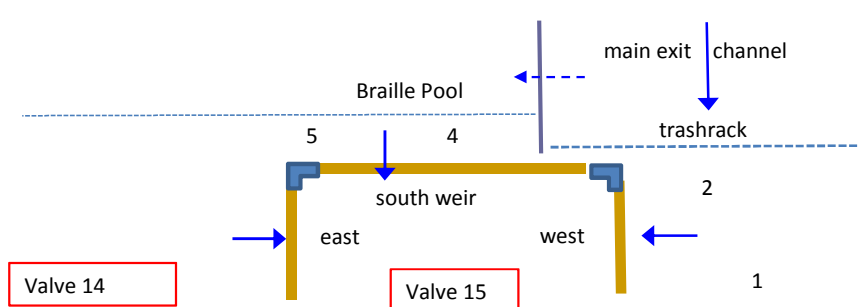


CURRENT Operation		Valve 15	75%
		Valve 14	0%
Depth Below Water (ft)	VELOCITIES (ft/s)		
	MEASURING LOCATION		
	1	1a	2
0.5	0.29	0.46	0.10
1.5	0.27	0.56	0.10
2.5	0.10		0.20
3.2	0.21		0.20
Average V	0.22	0.51	0.15
Average direction	↓	←	↖

Modified Operation		Valve 15	70%
		Valve 14	30%
Depth Below Water (ft)	VELOCITIES (ft/s)		
	MEASURING LOCATION		
	1	1a	2
0.5	0.29		0.00
1.5	0.23		0.19
2.5	0.19		0.22
3.2	0.17		0.29
Average V	0.22		0.18
Average direction	↓	←	↗

Centerline Velocities in Main Channel under Modified Operations

Depth Below Water (ft)	Current OP					
	Valve 15	75%	Valve 15	70%	Valve 15	60%
	Valve 14	0%	Valve 14	40%	Valve 14	50%
0.5		3.44		4.12		3.99
1.5		2.20		2.63		2.60
2.5		1.01		1.33		1.34
3.5		0.68		0.67		1.01
4.3		0.62		0.70		0.51
Average Velocity (ft/s)		1.59		1.89		1.89
Percent Above Normal		0.00		19%		19%

Water Level Data upstream of Stop Log weirs

Location	Distance from top of grating (ft)	(H) Depth above weir (ft)	surface cond.	(q) Unit discharge rate (cfs/ft)	Surface Velocity (ft/s)	Ws Elevations
1	1.04	1.00	no flow	3.31	3.31	44.0
2	1.08	0.96	fast	3.11	3.24	44.0
4	1.25	0.79	moderate	2.33	2.95	43.8
5	1.33	0.71	slow	1.97	2.79	43.8
Average head =		0.83	Total Q =	30.8	cfs	

Table 5-3 of King & Brater, "Handbook of Hydraulics"

Broad crested weir coefficient = 3.31

Edge contraction = 0.1 x H

3

13.9

35.2 2.534552

Weirs

		West	South	East	Total
ave H =	feet	0.98	0.82	0.71	
L =	feet	3	6.5	3	12.5
L' =	feet	2.90	6.42	2.93	12.25
Q weir =	cfs	9.3	15.8	5.8	30.8

ave DH = $(Q_{wr}/L'/C_w)^{0.67}$

ave DH = 0.83 feet

Weir Coeff. Factoring in Leakage = $C_{wl} = Q_{meas}/Q_{comp} * 3.31 =$

7.09 very high

Weir coefficient using max head =

5.39

Estimated Bypass Flume Diameter

Pipe = 14 Inch Sch 40 steel pipe

OD = 14.0 inches

Th = 0.437 inches

ID = 13.13 inches = 1.09 feet

66 4.3

38 2.5

Measured distances from walkway over exit channel to:

Bottom of channel raise 13.53 feet

distance to top of flume pipe at exit = 7.93 feet

depth in channel upstream of sill = 4.9 feet

depth in d/s elevated channel = 1.9 feet

distance to water surface elev = 11.63 feet

distance to flume invert = 9.0 feet

Height of flume invert above water = 2.6 feet

Elevation Difference in Pool Crest (DZ) = 1 foot

Orifice sqr Dim = 18 inch

Orifice Area (Ao) = 2.25 ft²

Orifice coeff (Cdo) = 0.67

 $Q_o = A_o * C_{do} * \sqrt{2g * (DZ)}$

Weir Crest Length (Lw) = 5 ft

Ladder Flow**Normal Case****Shad flow**

Ladder head (DH) = 1.0 feet Ladder hd (DHs) = 1.3 feet

Weir coeff (CW) = 5.07 Weir coeff (CWs) = 5.25

 $Q_w = L * C_w * (DH)^{1.5}$ $Q_w(shad) = L * C_{ws} * (D_sH)^{1.5} * \{1 - (DHs-1)/DHs\}^{1.5}^{0.385}$

Qo = Orifice flow = 12.1 cfs Qo (shad) = 12.1 cfs

Qw = Weir Flow = 25.4 cfs Qw (shad) = 37.2 cfs

Qt = Total Exit Ladder flow = 37.4 cfs QT (shad) = 49.3 cfs

Vp

measured = 66.1 cfs 14.16

ladder = 37.4 cfs

difference = 28.6 cfs

Valve 15

Butterfly Valve CD (ref: Figure 4.3, "Hydraulics of Pipelines", Tullis (1989))

Valve Loss Coeff = (Kv) $K_v = 1/CD^2 - 1$

Butterfly Discharge Coefficients

Operation case	Valve Opening	CD	Kv
Original Operation	55%	0.34	7.7
Current Operation	75%	0.50	3.0
Full open	100%	0.80	0.6
Intake loss coeff (Ki) =			0.15

Valve Opening	CD
0%	0.00
10%	0.02
20%	0.07
30%	0.14
40%	0.22
50%	0.30
60%	0.38
70%	0.46
80%	0.54
90%	0.64
100%	0.80

OD-15 = Valve 15 Pipe diameter = 30 in = 2.5 ft
 Wall thickness = 3/8 in = typical pipe wall thickness assumed
 ID - 15 = inside pipe Dia (vale 15) = 29.25 in = 2.44 ft
 A15 = Valve 15 Pipe area = 4.67 ft²

HL = Estimated Headloss through Valve = $(Q/A)^2 / 2g (K_v + K_i)$

HGL = HL + Z-15	Valve OP	Q	Vp	VH	HL	HGL	Measured	10/31/12
Z-15 = 33.25	75% open	65	13.9	3.01	9.5	42.7	43.0 ft	
	55% open	41	8.8	1.20	9.4	42.6		
	100% open	100	21.4	7.13	5.1	38.3		

Measured D/s of weir

below bottom of grating

10/24/12	19 inches >>	HGL =	43.4	Air bulking is factor
10/31/12	24 inches >>	HGL =	43.0	

Assume Valve HL is same $Q_1 = A_v CD_1 \cdot \sqrt{2gDH}$
 $Q_2 = A_v CD_2 \cdot \sqrt{2gDH}$

 $Q_1/Q_2 = CD_1/CD_2 = 0.68$

Vp (ft/s)

$Q_2 = 66.1$ cfs
 $Q_1 = Q_2 \cdot CD_1/CD_2 = 44.9$ cfs
 % Q reduction = 32%

Size Porosity Plates for Design Flow

Design Flow = 38.0 cfs, or Design Ladder Flow

	Open Length of Porosity Plates			Remaining open length of Stop Log weirs	
	South	west	sum	Prev sum	Remainder sum
Perf. height	1.5	3	4.5 ft	12.5	7.5

CW with leakage estimated = 7.09
 Assume with reduce leakage CWr = 4
 Ave DH = 0.83 ft
 Raise weirs 4 inches
 Revised DH = 0.50 ft
 Sum eff length $L' = L - 0.1 \cdot DH \cdot 2 = 7.40$ feet

$Q_{wr} = \text{New Weir Flow Rate} = C_{Wr} \cdot L' \cdot \text{Ave DH}^{1.5}$
 $Q_{wr} = 10.5$ cfs

 $Q_s = \text{Total Target Exit Discharge} = 38.0$ cfs

$Q_{pp} = \text{Net discharge through Porosity Plates} = Q_s - Q_{wr}$
 $Q_{pp} = 27.5$ cfs

Valve (Tullis) data reversed

CD	Valve Opening
0.00	0%
0.02	10%
0.07	20%
0.14	30%
0.22	40%
0.30	50%
0.38	60%
0.46	70%
0.54	80%
0.64	90%
0.80	100%

Average
 Channel Velocity
 1.0 ft/s

Flow depth = 4.9 ft
 Assume differential = 2.5 ft Valve can be adjusted to attain this differential
 level d/s of weirs = 2.4 ft HGL = 41.4 ft
 Valve Head loss = 8.15 feet
 Required KV = 7.76 >> CD = 0.34 >>> Valve Opening = 55% open

Hole diameter (Do) = 3 inches Hole area(Ao) = 7.07 in^2 = 0.049 ft^2
 Discharge coeff (CDo) = 0.63
 Head diff = minimum(Flow depth - WS d/s of weir, flow depth - hole elev)

Assume square grid spacing Set Spacing at 6 inches Porosity = 20%
 Number of rows = 9
 Number of holes per row N Discharge = 27.4
 Height (ft) 4 9 check diff from target % diff = 0%
 Height (ft) 5 6

Row Discharge = $Q_r = CD * \Sigma A_o * \sqrt{2g * DH}$

$\Sigma A_o = N * A_o$

	Elev above floor (ft)	Area of Holes (ft^2)	Head diff (ft)	Row Discharge Rate (cfs)	Sum Q (cfs)
1 Row 1	0.25	0.442	2.50	3.53	3.53
2 Row 2	0.75	0.442	2.50	3.53	7.06
3 Row 3	1.25	0.442	2.50	3.53	10.59
4 Row 4	1.75	0.442	2.50	3.53	14.13
5 Row 5	2.25	0.442	2.50	3.53	17.66
6 Row 6	2.75	0.442	2.15	3.28	20.93
7 Row 7	3.25	0.442	1.65	2.87	23.80
8 Row 8	3.75	0.442	1.15	2.40	26.20
9 Row 9	4.25	0.295	0.65	1.20	27.40
10 Row 10					
11 Row 11					
12 Row 12					

Check Shad Condition (Weir Head = 1.3 feet)

Increased head = 0.3
 Flow depth = 5.2 ft
 Assume differential = 2.2 ft
 level d/s of weirs = 3 ft

Weirs

Ave DH with normal Flow = 0.50 ft
 Revised DH with increase head 0.80
 Sum eff length $L' = L - 0.1 * DH * 2 = 7.34$ feet

$Q_{wr} = \text{New Weir Flow Rate} = C_{Wr} * L' * \text{Ave DH}^{1.5}$

$Q_{wr} = 21.2$ cfs

$Q_s = \text{Total Target Exit Discharge} = 49.3$ cfs
 Average Channel Velocity 1.3 ft/s

$Q_{pp} = Q_s - Q_{wr} = 28.1$ cfs

Valve can be adjusted to attain this differential

HGL = 42 ft
 Valve Head loss = 8.75 feet
 Required KV = 4.90 >> CD = 0.41 >>> Valve Opening = 64% open

Same square grid spacing (Shad Condition continued) 6 inches Porosity = 20%
 Number of rows = 10
 Number of holes per row N
 Height 4 9
 Height 5 6

Discharge = 28.14 % diff = 0%

	Elev above floor (ft)	Area of Holes (ft^2)	Head diff (ft)	Row Discharge Rate (cfs)	Sum Q (cfs)
1 Row 1	0.25	0.442	2.20	3.31	3.31
2 Row 2	0.75	0.442	2.20	3.31	6.63
3 Row 3	1.25	0.442	2.20	3.31	9.94
4 Row 4	1.75	0.442	2.20	3.31	13.25
5 Row 5	2.25	0.442	2.20	3.31	16.56
6 Row 6	2.75	0.442	2.20	3.31	19.88
7 Row 7	3.25	0.442	1.95	3.12	23.00
8 Row 8	3.75	0.442	1.45	2.69	25.69
9 Row 9	4.25	0.295	0.95	1.45	27.14
10 Row 10	4.75	0.295	0.45	1.00	28.14
11 Row 11					
12 Row 12					

Check: No Flow Change Scenario

Increased head = 0.1 ft
 Flow depth = 5 ft
 Assume PP differential = 4.7 ft
 level d/s of weirs = 0.3 ft
 Weirs
 Remove 4" raise
 Ave DH with normal Flow = 0.83 ft
 Revised DH with increase head 0.93
 Sum eff length $L' = L - 0.1 * DH * 2 =$ 7.31 feet

$Q_{wr} = \text{New Weir Flow Rate} = C_{wr} * L' * \text{Ave DH}^{1.5}$

$Q_{wr} =$ 26.7 cfs

$Q_s = \text{Total Target Exit Discharge} =$

68.0 cfs

Average
Channel Velocity
1.7 ft/s

$Q_{pp} = Q_s - Q_{wr}$ 41.3 cfs

Valve can be adjusted to attain this differential

HGL = 39.3 ft

Valve Head loss = 6.05 feet

Required KV = 1.68 >> CD = 0.61 >>> Valve Opening = 87% open

Same square grid spacing (no Flow Change continued) 6 inches Porosity = 20%

Number of rows = 10

Number of holes per row Discharge = 41.97 % diff = -2%

Height 4 9

Height 5 6

	Elev above floor (ft)	Area of Holes (ft^2)	Head diff (ft)	Row Discharge Rate (cfs)	Sum Q (cfs)
1 Row 1	0.25	0.442	4.70	4.84	4.84
2 Row 2	0.75	0.442	4.70	4.84	9.68
3 Row 3	1.25	0.442	4.70	4.84	14.53
4 Row 4	1.75	0.442	4.70	4.84	19.37
5 Row 5	2.25	0.442	4.70	4.84	24.21
6 Row 6	2.75	0.442	4.70	4.84	29.05
7 Row 7	3.25	0.442	4.70	4.84	33.90
8 Row 8	3.75	0.442	4.70	4.84	38.74
9 Row 9	4.25	0.295	4.70	3.23	41.97
10 Row 10	4.75	0.295			41.97
11 Row 11					
12 Row 12					

Flood Scenario

Assume current discharge rounded up to nearest 10 cfs

Assume all perforation are plugged

All flow over top of weirs and Perf plates

Q = 70.0 cfs WS = 5.87 ft

Weir Length L (ft)	CW	Weir Ht Zwr (ft)	DH (ft)	eff length L' (ft)	Q (cfs)
4.5	3.3	5	0.87	4.3	11.6
8	4.0	4.33	1.54	7.7	58.6
sum					70.1 cfs
diff =					0.1

Required Flow for recovery boxes

1 gpm per 15 lbs of fish
5% increase for every degree above 50 degrees

maximum water temp = 72 deg Base temp = 50 deg

Average fish weight = 37 lbs

number of fish/box = 1

Nb=number of boxes = 4 = number of inflow pipes

Total water supply = 1 gpm/15 lbs * 4 boxes * 37 lbs * (1 + (72 - 50) * 5%)

Total water supply = 20.72 gpm = 0.04616435 cfs

V = outlet velocity = $Q_t/N_p/(\pi D^2/4)$

Pipe Diameter (inches)			Thick-ness	Velocity (ft/s)
Nominal	OD	ID		
1	1.32	1.05	0.133	1.9
1.25	1.66	1.38	0.140	1.1
1.5	1.90	1.61	0.145	0.8
2	2.38	2.07	0.154	0.5
2.5	2.88	2.47	0.203	0.3
3	3.50	3.07	0.216	0.2

Elevation Difference in Pool Crest (DZ) = 1
 Orifice sqr Dim = 18 inch
 Orifice Area (Ao) = 2.25 ft²
 Orifice coeff (Cdo) = 0.67 $Q_o = A_o * C_{do} * \sqrt{2g * (DZ)}$
 Weir Crest Length (Lw) = 5 ft

Ladder Flow**Normal Case**

Ladder head (DH) =	1.0 feet	0.8	5.05	0.1
Weir coeff (CW) =	5.07	1	5.07	0.6
$Q_w = L * C_w * (DH)^{1.5}$		1.3	5.25	3.8
Qo = Orifice flow =	12.1 cfs	1.5	6.01	4.0
Qw = Weir Flow =	25.4 cfs	1.7	6.80	
Qt = Total Exit Ladder flow =	37.4 cfs			

Backwater Profile for Exit Ladder to Pool 49 assuming Current Conditions

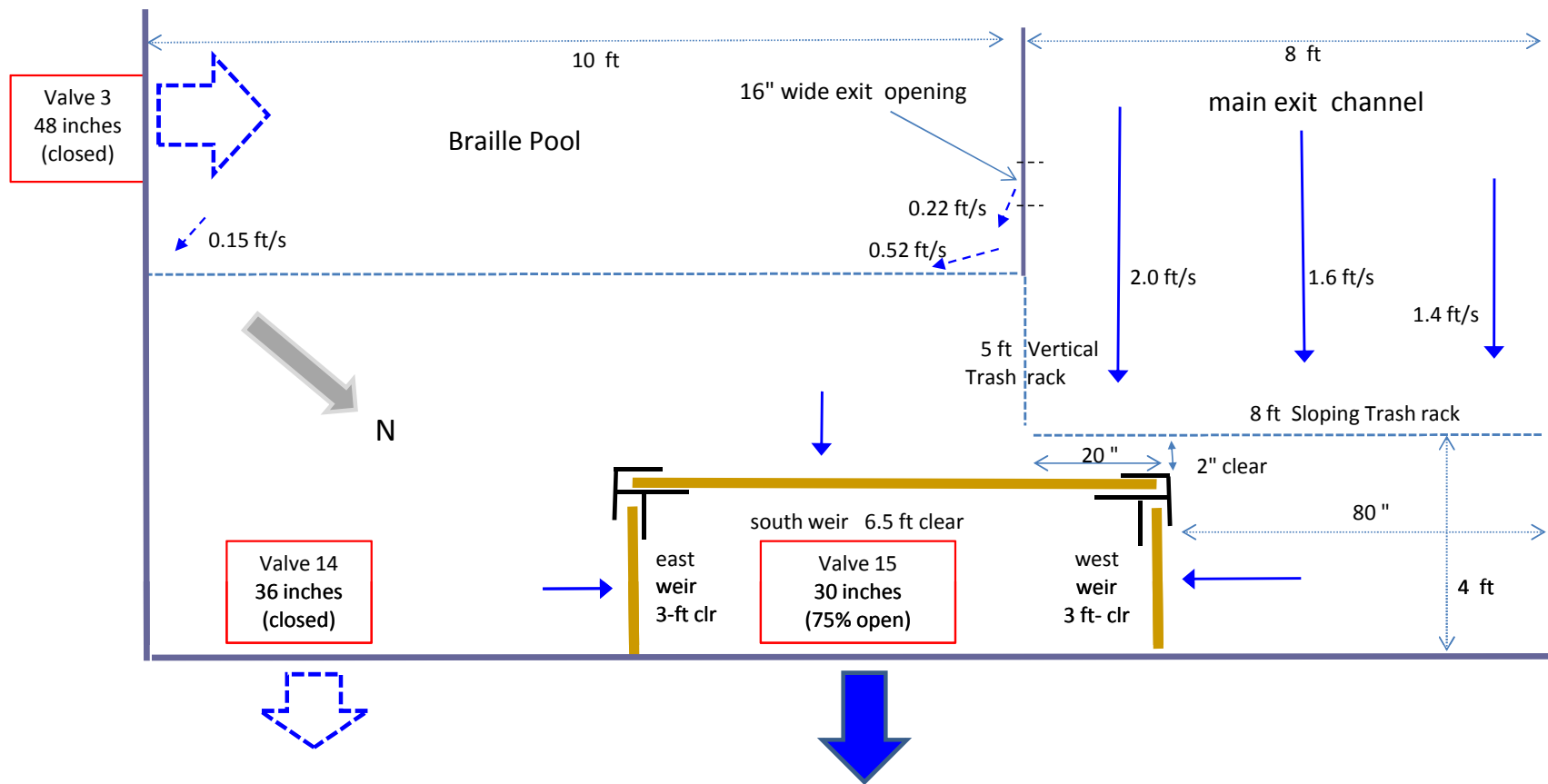
Q = 66.1 cfs
 D/s Depth = 4.9 ft WS EL = 43.9 ft

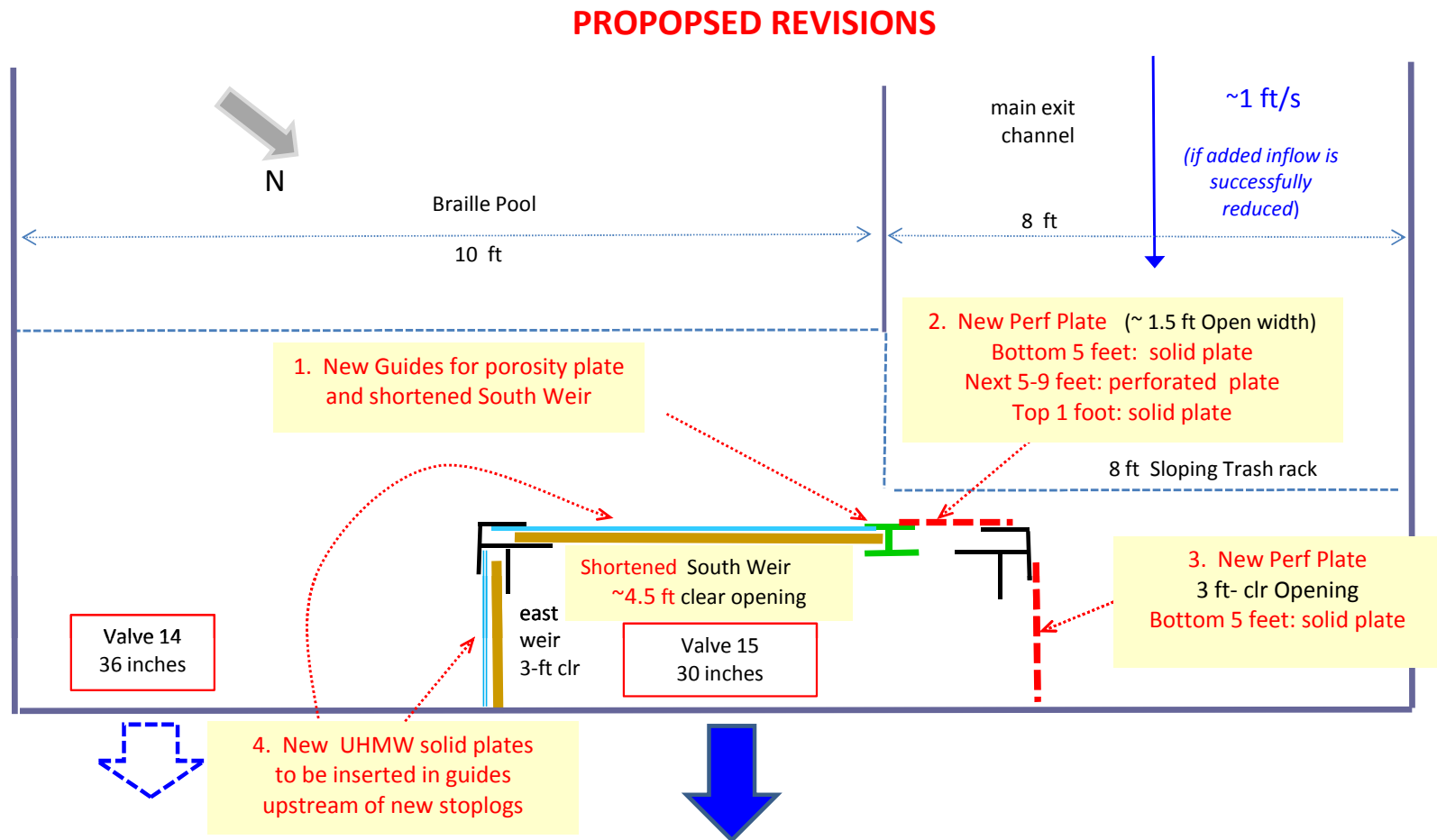
Weir	D/S WS EL	DH	U/S WS	Hu	DH	Qo	Hu	Cw	Qw
44	43.90		1.55	45.45		1	12.1	0.90	5.06 21.6
45	45.45		1.07	46.52		1.55	15.1	2.00	8.00 108.7
46	46.52		1.01	47.54		1.07	12.5	1.59	6.38 59.2
47	47.54		1.00	48.54		1.01	12.2	1.55	6.21 55.0
48	48.54		1.00	49.54		1.00	12.1	1.54	6.18 54.2
49	49.54		1.00	50.54	1.5	1.00	12.1	1.54	6.17 54.0

Average Exit Channel Velocities

Case	Flow Rate (cfs)	Channel Velocities (ft/s)	
		Deep Section	Shallow Section
Current OP	66	1.7	4.3
Design	38	1.0	2.5

EXISTING OPERATION WITH DIMENSIONS AND DEPTH AVERAGED VELOCITIES





Bonneville AFF : Flume Calcs			INNER FLUME		
Assumptions					
Pipe thickness	0.437	inch	g =	32.2 ft/s ²	
Pipe O.D. =	14	inches	SDR 40 PVC		
Mannings n =	0.010	(PVC)			
			Diameter =	13.13 inches =	1.1 ft
			Flow rate	110 gpm =	0.25 cfs
Nominal Flow Rate			Total L	39.0 feet	
	Z(elevation)		Location		Slope
U/s Flume IE. Elev	49.0 ft	X 1	0 feet	interval 1	0.11
DS end bend 1	46.6 ft	X 2	21.5 feet	interval 2	0.12
US end Bend 2	44.5 ft	X 3	39.0 feet		
	DEPTH		Velocity		Normal Depth
	(ft)	(in)	(ft/s)		
End of 1st Slope :	0.086	1.04	7.11		0.086 ft
End of 2nd Slope:	0.084	1.01	7.36		0.084 ft
minimum water depth:					
0.084 ft =	1.0	inches			
min. WS elevation =	43.90	ft	Min FROUDE No. =	3.5	(d/s of 1rst 5 feet)
Jet Impact Velocity					
Beta = atan (slope)	0.120	radians =	6.9	degrees	
Total velocity (Vt) at end of flume =			7.36	ft/s	
vertical component (Vzi) = Vt * sin(beta)			0.88	ft/s	
horizontal comp (Vx) = Vt cos (beta)			7.30	ft/s	
Vertical velocity (Vzi) at impact = sqrt(2g*(Z2-z3+y2/2) * Vz'			9.6	ft/s	
Total Impact Velocity (Vti) at Impact = sqrt(Vzi^2 + Vx^2) =			12.1	ft/s	
βi = Angle of Impact with Respect to horixontal =	0.92	rads =	52.7	degrees	
Vti =	12.1	ft/s	OK, Vti is less than 25 ft/s		

drop in pipe = 2.00 feet

Normal Depth	Yn (in)	Locaton	X (feet)	Z elevation (feet)	Depth (in)	Velocity (ft)	FR
1.0	X 1	0	49.0	1.71	3.4	1.9	
1.0	X 2	21.5	46.6	1.04	7.1	5.2	
	X 3	39.0	44.5	1.01	7.4	5.43	

RESULTS OF DIFFERENT FLOW CONDITIONS

Depth of Flow (in)	Discharge		Velocity (ft/s)		Impact Angle (deg)
	gpm	cfs	Exit	Impact	
0.5	25	0.06	4.7	9.1	59
1.0	110	0.25	7.4	12.1	53
1.5	240	0.53	9.3	14.4	50
2.0	450	1.00	11.0	16.7	49

EQUATIONS FOR FLUME CALCULATIONS

Equation for Water Depth

Reference: Henderson (1966), *Open Channel Flow*, Eq 7-52

$$\frac{dy}{dx} = \frac{S_o - S_f}{1 - Fr^2}$$

in which;

$$\begin{aligned} \frac{dy}{dx} &= \text{change in water depth with respect to channel length,} \\ S_o &= \text{channel slope,} \\ S_f &= \text{friction slope} \\ &= \frac{Q^2 n^2}{C^2 A^2 R h^{1.33}} \\ Q &= \text{flow rate (cfs) in channel at location x,} \\ g &= \text{gravity = 32.2 ft/s}^2 \\ A &= \text{cross-sectional flow area at location x (ft}^2\text{)} \\ &= \frac{D^2 \cdot (\beta - \cos\beta \cdot \sin\beta)}{4} \\ Fr^2 &= \text{Froude number squared} \\ &= \frac{TQ^2}{gA^3} \end{aligned}$$

and:

$$\begin{aligned} y &= \text{flow depth (ft)} \\ D &= \text{Inside Diameter of Pipe Flume (ft)} \\ n &= \text{Manning roughness factor,} \\ C &= \text{coefficient (1.486 for English units, 1 for metric units).} \\ \beta &= \cos^{-1}\left(1 - \frac{2 \cdot y}{D}\right) \quad (\text{radians}) \\ Rh &= \text{hydraulic radius (ft) = area/wetted perimeter,} \\ &= A/P \\ P &= \text{wetted perimeter (ft) = } D \cdot \beta \\ T &= \text{Top width of flow (ft)} \\ &= D \cdot \sin(\beta) \end{aligned}$$

Computation Procedure Using 4th Order Runge-Kutta Methods

Assume initial depth $Y_1 = (Y_c + Y_n)/2$ due to energy of false weir at u/s end

Y_n = normal depth (ft) = depth at which $SF = S_o$

Y_c = critical depth (ft) = depth at which $FR^2 = 1$

Given: $D, Q, Z, X, DX, S_o, g, n, C$

From Y_1 , Compute $\beta, A, V, P, Rh, 1-FR^2, SF$ and Dy/Dx based on above equations

$X + DX$ = next X location for depth computation (ft)

Fourth Order Runge- Kutta Calculation for Y at $X + DX$:

$$DY_1 = \text{1st estimate of change in } Y \text{ over } DX; \quad DY_1 = DX * (Dy/DX)_1$$

$$DY_2 = \text{2nd estimate of change in } Y \text{ over } DX; \quad DY_2 = DX * (Dy/DX)_2$$

$$DY_3 = \text{3rd estimate of change in } Y \text{ over } DX; \quad DY_3 = DX * (Dy/DX)_3$$

$$DY_4 = \text{4th estimate of change in } Y \text{ over } DX; \quad DY_4 = DX * (Dy/DX)_4$$

$$DY = (DY_1 + 2 * DY_2 + 2 * DY_3 + DY_4) / 6$$

$$Y_{i+1} = Y_i + DY$$

$$DY/DX_1 \text{ based on } Y_i \text{ at } X$$

$$DY/DX_2 \text{ based on } Y_i + DY_1/2 \text{ at } X + DX/2$$

$$DY/DX_3 \text{ based on } Y_i + DY_2/2 \text{ at } X + DX/2$$

$$DY/DX_4 \text{ based on } Y_i + DY_3 \text{ at } X + DX$$

LEG 1 SUPERCRITICAL FLOW COMPUTATIONS*Existing Pipe*

X1 = 0.0 ft **D = 1.094 ft**
X2 = 21.5 ft **Q = 0.245 cfs** **z1 = 49.0 ft**
 Length = 21.5 ft **Z2 = 46.6 ft**
 Yc = 0.1984 **So = 0.1100**
Y1 = 0.14 **Yn = 0.0860**
Dx = 0.22 ft
n = 0.01 **g = 32.2** $\rho = 1.94$
C = 1.486 **2g = 64.4** $\gamma = 62.40$

Critical depth for Circular channels

g = 32.2 ft/sec^2 **Tolerance**
D = 1.094 ft **1E-08**

Critical Depth supercrit	Q	Yc	Critical flow area	Critical velocity	Top width	error	0
	0.245	0.198	0.116	2.11	0.84		
Normal Depth supercrit	Q	Yn	Dia	slope	n		
	0.245	0.086	1.094	11%	0.01		

end: 0.0863 0.245 7.11

x (ft)	Z (ft)	y (ft)	Q (cfs)	beta (rads)	area (ft^2)	V (ft/s)	WS EL (ft)	EGL (ft)	T	FR	1-FR^2	P (ft)	Rh (ft)	SF	dY1/dx	DY (ft)
0.00	48.97	0.142	0.245	0.738	0.0718	3.41	49.11	49.29	0.736	1.93	-2.712	0.807	0.089	0.013	-0.036	0.000
0.22	48.94	0.136	0.245	0.721	0.0674	3.64	49.08	49.28	0.722	2.10	-3.408	0.789	0.085	0.016	-0.028	-0.006
0.43	48.92	0.131	0.245	0.706	0.0636	3.86	49.05	49.28	0.710	2.27	-4.154	0.773	0.082	0.019	-0.022	-0.005
0.65	48.90	0.127	0.245	0.694	0.0606	4.05	49.02	49.28	0.700	2.42	-4.879	0.759	0.080	0.022	-0.018	-0.004
0.86	48.87	0.123	0.245	0.684	0.0581	4.22	48.99	49.27	0.691	2.57	-5.585	0.748	0.078	0.024	-0.015	-0.003
1.08	48.85	0.120	0.245	0.675	0.0560	4.38	48.97	49.27	0.683	2.70	-6.275	0.738	0.076	0.027	-0.013	-0.003
1.29	48.82	0.117	0.245	0.667	0.0542	4.53	48.94	49.26	0.677	2.82	-6.949	0.730	0.074	0.030	-0.012	-0.002
1.51	48.80	0.115	0.245	0.660	0.0526	4.66	48.92	49.25	0.671	2.93	-7.607	0.722	0.073	0.032	-0.010	-0.002
1.72	48.78	0.113	0.245	0.654	0.0512	4.79	48.89	49.25	0.665	3.04	-8.250	0.715	0.072	0.035	-0.009	-0.002
1.94	48.75	0.111	0.245	0.648	0.0500	4.90	48.86	49.24	0.661	3.14	-8.877	0.709	0.070	0.037	-0.008	-0.002
2.15	48.73	0.109	0.245	0.643	0.0489	5.02	48.84	49.23	0.656	3.24	-9.488	0.704	0.069	0.040	-0.007	-0.002
2.37	48.71	0.108	0.245	0.639	0.0479	5.12	48.81	49.22	0.652	3.33	-10.083	0.699	0.069	0.042	-0.007	-0.001
2.58	48.68	0.106	0.245	0.634	0.0470	5.22	48.79	49.21	0.648	3.42	-10.663	0.694	0.068	0.045	-0.006	-0.001
2.80	48.66	0.105	0.245	0.631	0.0462	5.31	48.76	49.20	0.645	3.50	-11.227	0.690	0.067	0.047	-0.006	-0.001
3.01	48.64	0.104	0.245	0.627	0.0454	5.40	48.74	49.19	0.642	3.57	-11.775	0.686	0.066	0.049	-0.005	-0.001
3.23	48.61	0.103	0.245	0.624	0.0447	5.48	48.71	49.18	0.639	3.65	-12.307	0.682	0.066	0.051	-0.005	-0.001
3.44	48.59	0.102	0.245	0.621	0.0441	5.56	48.69	49.17	0.636	3.72	-12.823	0.679	0.065	0.054	-0.004	-0.001
3.66	48.56	0.101	0.245	0.618	0.0435	5.63	48.67	49.16	0.633	3.78	-13.324	0.676	0.064	0.056	-0.004	-0.001
3.87	48.54	0.100	0.245	0.615	0.0430	5.70	48.64	49.15	0.631	3.85	-13.810	0.673	0.064	0.058	-0.004	-0.001
4.09	48.52	0.099	0.245	0.612	0.0425	5.77	48.62	49.13	0.629	3.91	-14.280	0.670	0.063	0.060	-0.004	-0.001
4.30	48.49	0.099	0.245	0.610	0.0420	5.83	48.59	49.12	0.627	3.97	-14.736	0.667	0.063	0.061	-0.003	-0.001
4.52	48.47	0.098	0.245	0.608	0.0416	5.89	48.57	49.11	0.625	4.02	-15.177	0.665	0.063	0.063	-0.003	-0.001
4.73	48.45	0.097	0.245	0.606	0.0412	5.95	48.54	49.09	0.623	4.07	-15.603	0.663	0.062	0.065	-0.003	-0.001
4.95	48.42	0.097	0.245	0.604	0.0408	6.00	48.52	49.08	0.621	4.12	-16.015	0.661	0.062	0.067	-0.003	-0.001

Internal row calculations not shown for brevity

20.00	46.77	0.086	0.245	0.570	0.0345	7.09	46.85	47.63	0.590	5.17	-25.697	0.623	0.055	0.108	0.000	0.000
20.21	46.74	0.086	0.245	0.570	0.0345	7.10	46.83	47.61	0.590	5.17	-25.719	0.623	0.055	0.108	0.000	0.000
20.43	46.72	0.086	0.245	0.570	0.0345	7.10	46.81	47.59	0.590	5.17	-25.740	0.623	0.055	0.108	0.000	0.000
20.64	46.70	0.086	0.245	0.569	0.0345	7.10	46.78	47.57	0.590	5.17	-25.760	0.623	0.055	0.108	0.000	0.000
20.86	46.67	0.086	0.245	0.569	0.0345	7.10	46.76	47.54	0.590	5.17	-25.779	0.623	0.055	0.108	0.000	0.000
21.07	46.65	0.086	0.245	0.569	0.0345	7.10	46.74	47.52	0.590	5.18	-25.797	0.623	0.055	0.108	0.000	0.000
21.29	46.63	0.086	0.245	0.569	0.0345	7.11	46.71	47.50	0.590	5.18	-25.814	0.623	0.055	0.108	0.000	0.000
21.50	46.60	0.086	0.245	0.569	0.0345	7.11	46.69	47.47	0.590	5.18	-25.831	0.623	0.055	0.108	0.000	0.000

LEG 2 SUPERCRITICAL FLOW COMPUTATIONS*New Pipe Extension*

X2 = 21.5 ft **D =** 1.094 ft
X3 = 39.0 ft **Q =** 0.245 cfs **Z2=** 46.6 ft
Length = 17.5 ft **Z3=** 44.5 ft
 20 **So =** 0.1200
Y1 = 0.09 Yc = 0.1984
Dx = 0.88 ft Yn = 0.0842
n = 0.01 **g =** 32.2 $\rho =$ 1.94
C = 1.486 **2g =** 64.4 $\gamma =$ 62.40

Critical depth for Circular channels

g = 32.2 ft/sec² Tolerance
D = 1.094 ft 1E-08

Critical Depth supercrit	Q	Yc	Critical flow area	Critical velocity	Top width	error	0
	0.245	0.198	0.116	2.11	0.84		
Normal Depth supercrit	Q	Yn	Dia	slope	n		
	0.245	0.084	1.094	12%	0.01		

End: 0.0843 0.245 7.36

x	Z	y (ft)	Q	beta (rads)	area	V	ws	EGL	T	FR	1-FR^2	P	Rh	SF	dY1/dx	DY	1
21.50	46.60	0.086	0.245	0.569	0.0345	7.11	46.69	47.47	0.590	5.18	-25.831	0.623	0.055	0.108	0.000	0.000	
21.50	46.60	0.086	0.245	0.569	0.0345	7.11	46.69	47.47	0.590	5.18	-25.834	0.623	0.055	0.108	0.000	0.000	
21.51	46.60	0.086	0.245	0.569	0.0345	7.11	46.69	47.47	0.590	5.18	-25.837	0.623	0.055	0.108	0.000	0.000	
21.51	46.60	0.086	0.245	0.569	0.0345	7.11	46.69	47.47	0.590	5.18	-25.839	0.623	0.055	0.108	0.000	0.000	
21.52	46.60	0.086	0.245	0.569	0.0345	7.11	46.68	47.47	0.590	5.18	-25.842	0.623	0.055	0.108	0.000	0.000	
21.52	46.60	0.086	0.245	0.569	0.0345	7.11	46.68	47.47	0.590	5.18	-25.845	0.623	0.055	0.108	0.000	0.000	
21.61	46.59	0.086	0.245	0.569	0.0345	7.11	46.67	47.46	0.590	5.18	-25.845	0.623	0.055	0.108	0.000	0.000	
21.70	46.58	0.086	0.245	0.569	0.0345	7.11	46.66	47.45	0.589	5.19	-25.892	0.623	0.055	0.109	0.000	0.000	
21.79	46.57	0.086	0.245	0.569	0.0344	7.12	46.65	47.44	0.589	5.19	-25.939	0.622	0.055	0.109	0.000	0.000	
21.87	46.56	0.086	0.245	0.569	0.0344	7.12	46.64	47.43	0.589	5.19	-25.985	0.622	0.055	0.109	0.000	0.000	
21.96	46.55	0.086	0.245	0.569	0.0344	7.13	46.63	47.42	0.589	5.20	-26.031	0.622	0.055	0.109	0.000	0.000	
22.05	46.54	0.086	0.245	0.569	0.0344	7.13	46.62	47.41	0.589	5.20	-26.075	0.622	0.055	0.109	0.000	0.000	
22.14	46.53	0.086	0.245	0.569	0.0343	7.14	46.61	47.40	0.589	5.21	-26.119	0.622	0.055	0.110	0.000	0.000	
22.22	46.51	0.086	0.245	0.568	0.0343	7.14	46.60	47.39	0.589	5.21	-26.162	0.622	0.055	0.110	0.000	0.000	
22.31	46.50	0.086	0.245	0.568	0.0343	7.14	46.59	47.38	0.589	5.22	-26.204	0.622	0.055	0.110	0.000	0.000	
23.19	46.40	0.086	0.245	0.567	0.0341	7.18	46.48	47.29	0.588	5.25	-26.588	0.620	0.055	0.112	0.000	0.000	
24.06	46.29	0.085	0.245	0.566	0.0340	7.21	46.38	47.19	0.587	5.28	-26.908	0.620	0.055	0.113	0.000	0.000	
24.94	46.19	0.085	0.245	0.566	0.0339	7.24	46.27	47.09	0.586	5.31	-27.176	0.619	0.055	0.114	0.000	0.000	
25.81	46.08	0.085	0.245	0.565	0.0338	7.26	46.17	46.99	0.586	5.33	-27.400	0.618	0.055	0.115	0.000	0.000	
26.69	45.98	0.085	0.245	0.565	0.0337	7.28	46.06	46.89	0.585	5.35	-27.586	0.618	0.055	0.116	0.000	0.000	
27.56	45.87	0.085	0.245	0.564	0.0336	7.29	45.96	46.78	0.585	5.36	-27.741	0.617	0.054	0.117	0.000	0.000	
28.44	45.77	0.085	0.245	0.564	0.0336	7.30	45.85	46.68	0.585	5.37	-27.871	0.617	0.054	0.117	0.000	0.000	
29.32	45.66	0.085	0.245	0.564	0.0335	7.31	45.75	46.58	0.584	5.38	-27.979	0.617	0.054	0.118	0.000	0.000	
30.19	45.56	0.085	0.245	0.563	0.0335	7.32	45.64	46.48	0.584	5.39	-28.068	0.616	0.054	0.118	0.000	0.000	
31.07	45.45	0.084	0.245	0.563	0.0334	7.33	45.54	46.37	0.584	5.40	-28.143	0.616	0.054	0.118	0.000	0.000	
31.94	45.35	0.084	0.245	0.563	0.0334	7.34	45.43	46.27	0.584	5.40	-28.205	0.616	0.054	0.119	0.000	0.000	
32.82	45.24	0.084	0.245	0.563	0.0334	7.34	45.33	46.16	0.584	5.41	-28.257	0.616	0.054	0.119	0.000	0.000	
33.69	45.14	0.084	0.245	0.563	0.0334	7.34	45.22	46.06	0.584	5.41	-28.300	0.616	0.054	0.119	0.000	0.000	
34.57	45.03	0.084	0.245	0.563	0.0334	7.35	45.12	45.96	0.584	5.42	-28.335	0.616	0.054	0.119	0.000	0.000	
35.44	44.93	0.084	0.245	0.563	0.0333	7.35	45.01	45.85	0.584	5.42	-28.365	0.615	0.054	0.119	0.000	0.000	
36.32	44.82	0.084	0.245	0.563	0.0333	7.35	44.91	45.75	0.583	5.42	-28.390	0.615	0.054	0.119	0.000	0.000	
37.19	44.72	0.084	0.245	0.563	0.0333	7.35	44.80	45.64	0.583	5.42	-28.410	0.615	0.054	0.120	0.000	0.000	
38.07	44.61	0.084	0.245	0.563	0.0333	7.36	44.70	45.54	0.583	5.42	-28.427	0.615	0.054	0.120	0.000	0.000	
38.94	44.51	0.084	0.245	0.562	0.0333	7.36	44.59	45.43	0.583	5.43	-28.441	0.615	0.054	0.120	0.000	0.000	

Bonneville AFF : Flume Calcs	<i>OUTER FLUME</i>
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OUTER FLUME

Assumptions

Pipe thickness **0.437** inch **g =** **32.2 ft/s²**
 Pipe O.D. = **14** inches SDR 40 PVC
Mannings n = **0.010** (PVC)

drop in pipe = 2.00 feet

Nominal Flow Rate

Diameter = 13.13 inches = 1.1 ft
Flow rate 20 gpm = 0.04 cfs
Total L 51.8 feet

	Z(elevation)		Location		Slope
U/s Flume IE. Elev	49.4 ft	X 1	0 feet	interval 1	0.11
DS end bend 1	46.6 ft	X 2	25.4 feet	interval 2	0.08
US end Bend 2	44.5 ft	X 3	51.8 feet		

Normal			Z			
Depth		X	elevation	Depth	Velocity	
Yn (in)	Locaton	(feet)	(feet)	(in)	(ft)	FR
0.5	X 1	0	49.4	0.73	2.1	1.9
0.5	X 2	25.4	46.6	0.46	4.3	4.7
	X 3	51.8	44.5	0.50	3.8	4.00

	DEPTH		Velocity	
	(ft)	(in)	(ft/s)	Normal Depth
End of 1st Slope :	0.039	0.46	4.25	0.039 ft
End of 2nd Slope:	0.042	0.50	3.80	0.042 ft

minimum water depth:

0.039 ft = 0.5 inches
min. WS elevation **43.90** ft Min FROUDE No. = 4.0 (d/s of 1st 5 feet)

Jet Impact Velocity

Beta = atan (slope)	0.080 radians =	4.6 degrees
Total velocity (Vt) at end of flume =		3.80 ft/s
vertical component (Vzi) = Vt * sin(beta)		0.30 ft/s
horizontal comp (Vx) = Vt cos (beta)		3.79 ft/s

Vertical velocity (Vzi) at impact = $\sqrt{2g \cdot (Z2 - z3 + y2/2)} \cdot Vz'$ 7.3 ft/s

Total Impact Velocity (Vti) at Impact = $\text{sqrt}(V_{zi}^2 + V_x^2) = 8.2 \text{ ft/s}$

$$\beta_i = \text{Angle of Impact with Respect to horizontal} = 1.09 \text{ rads} = 62.5 \text{ degrees}$$

Vti = 8.2 ft/s OK, Vti is less than 25 ft/s

RESULTS OF DIFFERENT FLOW CONDITIONS

Depth of Flow (in)	Discharge		Velocity (ft/s)		Impact Angle (deg)
	gpm	cfs	Exit	Impact	
0.5	20	0.04	3.8	8.2	62
1.0	100	0.22	6.2	10.7	55
1.5	210	0.47	7.8	12.6	52
2.0	400	0.89	9.5	14.7	50

EQUATIONS FOR FLUME CALCULATIONS

Equation for Water DepthReference: Henderson (1966), *Open Channel Flow*, Eq 7-52

$$\frac{dy}{dx} = \frac{S_o - S_f}{1 - Fr^2}$$

in which;

$\frac{dy}{dx}$ = change in water depth with respect to channel length,
 S_o = channel slope,
 S_f = friction slope

= $\frac{Q^2 n^2}{C^2 A^2 R h^{1.33}}$
 Q = flow rate (cfs) in channel at location x,
 g = gravity = 32.2 ft/s²
 A = cross-sectional flow area at location x (ft²)

$$D^2 \cdot \frac{(\beta - \cos\beta \cdot \sin\beta)}{4}$$

Fr^2 = Froude number squared
 = TQ^2 / gA^3

and:

y = flow depth (ft)
 D = Inside Diameter of Pipe Flume (ft)
 n = Manning roughness factor,
 C = coefficient (1.486 for English units, 1 for metric units).

β = $\cos^{-1}\left(1 - \frac{2 \cdot y}{D}\right)$ (radians)

Rh = hydraulic radius (ft) = area/wetted perimeter,
 A/P
 P = wetted perimeter (ft) = $D \cdot \beta$

T = Top width of flow (ft)
 $D \cdot \sin(\beta)$

Computation Procedure Using 4th Order Runge-Kutta MethodsAssume initial depth $Y_1 = (Y_c + Y_n)/2$ due to energy of false weir at u/s end Y_n = normal depth (ft) = depth at which $SF = S_o$ Y_c = critical depth (ft) = depth at which $FR^2 = 1$ Given: $D, Q, Z, X, DX, S_o, g, n, C$ From Y_1 , Compute $\beta, A, V, P, Rh, 1-FR^2, SF$ and Dy/Dx based on above equations $X + DX$ = next X location for depth computation (ft)Fourth Order Runge- Kutta Calculation for Y at $X + DX$: DY_1 = 1st estimate of change in Y over DX ; $DY_1 = DX * (Dy/DX)_1$ DY_2 = 2nd estimate of change in Y over DX ; $DY_2 = DX * (Dy/DX)_2$ DY_3 = 3rd estimate of change in Y over DX ; $DY_3 = DX * (Dy/DX)_3$ DY_4 = 4th estimate of change in Y over DX ; $DY_4 = DX * (Dy/DX)_4$ $DY = (DY_1 + 2 * DY_2 + 2 * DY_3 + DY_4) / 6$ $Y_{i+1} = Y_i + DY$ DY/DX_1 based on Y_i at X DY/DX_2 based on $Y_i + DY_1/2$ at $X + DX/2$ DY/DX_3 based on $Y_i + DY_2/2$ at $X + DX/2$ DY/DX_4 based on $Y_i + DY_3$ at $X + DX$

LEG 1 SUPERCRITICAL FLOW COMPUTATIONS*Existing Pipe*

X1 = 0.0 ft **D = 1.094 ft**
X2 = 25.4 ft **Q = 0.045 cfs** **z1 = 49.4 ft**
 Length = 25.4 ft **Z2 = 46.6 ft**
 Yc = 0.0837 **So = 0.1100**
Y1 = 0.06 **Yn = 0.0387**
Dx = 0.25 ft
n = 0.01 **g = 32.2** $\rho = 1.94$
C = 1.486 **2g = 64.4** $\gamma = 62.40$

Critical depth for Circular channels

g = 32.2 ft/sec^2 **Tolerance**
D = 1.094 ft **1E-08**

Critical Depth supercrit	Q	Yc	Critical flow area	Critical velocity	Top width	error
0.045	0.084	0.033	1.35	0.58	-2.22E-15	

Normal Depth supercrit	Q	Yn	Dia	slope	n
0.045	0.039	1.094	11%	0.01	

end: 0.0386 0.045 4.25

x (ft)	Z (ft)	y (ft)	Q (cfs)	beta (rads)	area (ft^2)	V (ft/s)	WS EL (ft)	EGL (ft)	T	FR	1-FR^2	P (ft)	Rh (ft)	SF	dY1/dx	DY (ft)	1
0.00	49.39	0.061	0.045	0.478	0.0207	2.15	49.46	49.53	0.503	1.86	-2.473	0.522	0.040	0.015	-0.038	0.000	
0.25	49.37	0.055	0.045	0.452	0.0177	2.52	49.42	49.52	0.478	2.31	-4.318	0.495	0.036	0.024	-0.020	-0.005	
0.51	49.34	0.051	0.045	0.435	0.0158	2.81	49.39	49.51	0.461	2.68	-6.166	0.476	0.033	0.034	-0.012	-0.003	
0.76	49.31	0.048	0.045	0.424	0.0146	3.04	49.36	49.50	0.450	2.97	-7.847	0.463	0.032	0.042	-0.009	-0.002	
1.02	49.28	0.046	0.045	0.415	0.0138	3.23	49.33	49.49	0.441	3.22	-9.371	0.454	0.030	0.050	-0.006	-0.002	
1.27	49.26	0.045	0.045	0.409	0.0132	3.38	49.30	49.48	0.435	3.43	-10.745	0.447	0.029	0.057	-0.005	-0.001	
1.52	49.23	0.044	0.045	0.404	0.0127	3.51	49.27	49.46	0.430	3.60	-11.975	0.441	0.029	0.063	-0.004	-0.001	
1.78	49.20	0.043	0.045	0.399	0.0123	3.62	49.24	49.45	0.425	3.75	-13.070	0.437	0.028	0.069	-0.003	-0.001	
2.03	49.17	0.042	0.045	0.396	0.0120	3.71	49.21	49.43	0.422	3.88	-14.040	0.433	0.028	0.074	-0.003	-0.001	
2.29	49.14	0.042	0.045	0.393	0.0118	3.79	49.19	49.41	0.419	3.99	-14.897	0.430	0.027	0.079	-0.002	-0.001	
2.54	49.12	0.041	0.045	0.391	0.0116	3.86	49.16	49.39	0.417	4.08	-15.649	0.428	0.027	0.083	-0.002	0.000	
2.79	49.09	0.041	0.045	0.389	0.0114	3.91	49.13	49.37	0.415	4.16	-16.309	0.426	0.027	0.087	-0.001	0.000	
3.05	49.06	0.041	0.045	0.387	0.0113	3.96	49.10	49.34	0.413	4.23	-16.886	0.424	0.027	0.090	-0.001	0.000	
3.30	49.03	0.040	0.045	0.386	0.0111	4.00	49.07	49.32	0.412	4.29	-17.389	0.422	0.026	0.092	-0.001	0.000	
3.56	49.00	0.040	0.045	0.385	0.0110	4.04	49.04	49.30	0.411	4.34	-17.827	0.421	0.026	0.095	-0.001	0.000	
3.81	48.98	0.040	0.045	0.384	0.0110	4.07	49.02	49.27	0.410	4.38	-18.207	0.420	0.026	0.097	-0.001	0.000	
4.06	48.95	0.040	0.045	0.383	0.0109	4.09	48.99	49.25	0.409	4.42	-18.537	0.419	0.026	0.099	-0.001	0.000	
4.32	48.92	0.040	0.045	0.382	0.0108	4.12	48.96	49.22	0.408	4.45	-18.823	0.418	0.026	0.100	-0.001	0.000	
4.57	48.89	0.039	0.045	0.382	0.0108	4.13	48.93	49.20	0.408	4.48	-19.071	0.418	0.026	0.101	0.000	0.000	
4.83	48.86	0.039	0.045	0.381	0.0107	4.15	48.90	49.17	0.407	4.50	-19.286	0.417	0.026	0.103	0.000	0.000	
5.08	48.84	0.039	0.045	0.381	0.0107	4.16	48.88	49.15	0.407	4.52	-19.471	0.417	0.026	0.104	0.000	0.000	
5.33	48.81	0.039	0.045	0.380	0.0107	4.18	48.85	49.12	0.406	4.54	-19.631	0.416	0.026	0.105	0.000	0.000	
5.59	48.78	0.039	0.045	0.380	0.0106	4.19	48.82	49.09	0.406	4.56	-19.769	0.416	0.026	0.105	0.000	0.000	
5.84	48.75	0.039	0.045	0.380	0.0106	4.20	48.79	49.07	0.406	4.57	-19.889	0.415	0.026	0.106	0.000	0.000	

Internal row calculations not shown for brevity

23.62	46.80	0.039	0.045	0.378	0.0105	4.25	46.84	47.12	0.404	4.65	-20.632	0.414	0.025	0.110	0.000	0.000	
23.88	46.77	0.039	0.045	0.378	0.0105	4.25	46.81	47.09	0.404	4.65	-20.632	0.414	0.025	0.110	0.000	0.000	
24.13	46.74	0.039	0.045	0.378	0.0105	4.25	46.78	47.06	0.404	4.65	-20.632	0.414	0.025	0.110	0.000	0.000	
24.38	46.71	0.039	0.045	0.378	0.0105	4.25	46.75	47.03	0.404	4.65	-20.632	0.414	0.025	0.110	0.000	0.000	
24.64	46.69	0.039	0.045	0.378	0.0105	4.25	46.72	47.00	0.404	4.65	-20.632	0.414	0.025	0.110	0.000	0.000	
24.89	46.66	0.039	0.045	0.378	0.0105	4.25	46.70	46.98	0.404	4.65	-20.632	0.414	0.025	0.110	0.000	0.000	
25.15	46.63	0.039	0.045	0.378	0.0105	4.25	46.67	46.95	0.404	4.65	-20.632	0.414	0.025	0.110	0.000	0.000	
25.40	46.60	0.039	0.045	0.378	0.0105	4.25	46.64	46.92	0.404	4.65	-20.632	0.414	0.025	0.110	0.000	0.000	

LEG 2 SUPERCRITICAL FLOW COMPUTATIONS*New Pipe Extension*

X2 = 25.4 ft **D =** 1.094 ft
X3 = 51.8 ft **Q =** 0.045 cfs **Z2 =** 46.6 ft
Length = 26.4 ft **Z3 =** 44.5 ft
 20 **So =** 0.0797
Y1 = 0.04 Yc = 0.0837
Dx = 1.32 ft Yn = 0.0417
n = 0.01 **g =** 32.2 $\rho =$ 1.94
C = 1.486 **2g =** 64.4 $\gamma =$ 62.40

Critical depth for Circular channels

g = 32.2 ft/sec² Tolerance
D = 1.094 ft 1E-08

Critical Depth supercrit	Q	Yc	Critical flow area	Critical velocity	Top width	error
0.045	0.045	0.084	0.033	1.35	0.58	-2.22E-15

Normal Depth supercrit	Q	Yn	Dia	slope	n
0.045	0.045	0.042	1.094	8%	0.01

End: 0.0417 0.045 3.80

x	Z	y (ft)	Q	beta (rads)	area	V	ws	EGL	T	FR	1-FR^2	P	Rh	SF	dY1/dx	DY	1
25.40	46.60	0.039	0.045	0.378	0.0105	4.25	46.64	46.92	0.404	4.65	-20.632	0.414	0.025	0.110	0.001	0.000	
25.41	46.60	0.039	0.045	0.378	0.0105	4.25	46.64	46.92	0.404	4.65	-20.608	0.414	0.025	0.110	0.001	0.000	
25.41	46.60	0.039	0.045	0.378	0.0105	4.25	46.64	46.92	0.404	4.65	-20.584	0.414	0.025	0.110	0.001	0.000	
25.42	46.60	0.039	0.045	0.378	0.0105	4.25	46.64	46.92	0.404	4.64	-20.560	0.414	0.025	0.110	0.001	0.000	
25.43	46.60	0.039	0.045	0.378	0.0105	4.24	46.64	46.92	0.404	4.64	-20.537	0.414	0.025	0.109	0.001	0.000	
25.44	46.60	0.039	0.045	0.378	0.0105	4.24	46.64	46.92	0.404	4.64	-20.513	0.414	0.025	0.109	0.001	0.000	
25.57	46.59	0.039	0.045	0.378	0.0105	4.24	46.63	46.91	0.404	4.64	-20.513	0.414	0.025	0.109	0.001	0.000	
25.70	46.58	0.039	0.045	0.379	0.0106	4.21	46.62	46.89	0.405	4.59	-20.108	0.415	0.025	0.107	0.001	0.000	
25.83	46.57	0.039	0.045	0.380	0.0106	4.18	46.61	46.88	0.406	4.55	-19.735	0.416	0.026	0.105	0.001	0.000	
25.96	46.56	0.039	0.045	0.381	0.0107	4.16	46.60	46.86	0.407	4.52	-19.391	0.417	0.026	0.103	0.001	0.000	
26.10	46.55	0.039	0.045	0.382	0.0108	4.13	46.59	46.85	0.408	4.48	-19.073	0.418	0.026	0.101	0.001	0.000	
26.23	46.54	0.040	0.045	0.382	0.0108	4.11	46.58	46.84	0.408	4.45	-18.779	0.418	0.026	0.100	0.001	0.000	
26.36	46.53	0.040	0.045	0.383	0.0109	4.09	46.56	46.82	0.409	4.42	-18.508	0.419	0.026	0.098	0.001	0.000	
26.49	46.51	0.040	0.045	0.384	0.0109	4.07	46.55	46.81	0.410	4.39	-18.257	0.420	0.026	0.097	0.001	0.000	
26.62	46.50	0.040	0.045	0.384	0.0110	4.05	46.54	46.80	0.410	4.36	-18.025	0.420	0.026	0.096	0.001	0.001	
27.94	46.40	0.041	0.045	0.389	0.0114	3.93	46.44	46.68	0.414	4.18	-16.467	0.425	0.027	0.087	0.000	0.001	
29.26	46.29	0.041	0.045	0.391	0.0115	3.86	46.34	46.57	0.417	4.09	-15.730	0.427	0.027	0.083	0.000	0.000	
30.58	46.19	0.041	0.045	0.392	0.0116	3.83	46.23	46.46	0.418	4.05	-15.375	0.429	0.027	0.082	0.000	0.000	
31.89	46.08	0.042	0.045	0.392	0.0117	3.82	46.13	46.35	0.418	4.03	-15.202	0.429	0.027	0.081	0.000	0.000	
33.21	45.98	0.042	0.045	0.393	0.0117	3.81	46.02	46.25	0.418	4.01	-15.118	0.429	0.027	0.080	0.000	0.000	
34.53	45.87	0.042	0.045	0.393	0.0117	3.81	45.92	46.14	0.419	4.01	-15.077	0.430	0.027	0.080	0.000	0.000	
35.85	45.77	0.042	0.045	0.393	0.0117	3.80	45.81	46.04	0.419	4.01	-15.057	0.430	0.027	0.080	0.000	0.000	
37.16	45.66	0.042	0.045	0.393	0.0117	3.80	45.71	45.93	0.419	4.01	-15.048	0.430	0.027	0.080	0.000	0.000	
38.48	45.56	0.042	0.045	0.393	0.0117	3.80	45.60	45.82	0.419	4.01	-15.043	0.430	0.027	0.080	0.000	0.000	
39.80	45.45	0.042	0.045	0.393	0.0117	3.80	45.50	45.72	0.419	4.01	-15.041	0.430	0.027	0.080	0.000	0.000	
41.12	45.35	0.042	0.045	0.393	0.0117	3.80	45.39	45.61	0.419	4.00	-15.039	0.430	0.027	0.080	0.000	0.000	
42.43	45.24	0.042	0.045	0.393	0.0117	3.80	45.29	45.51	0.419	4.00	-15.039	0.430	0.027	0.080	0.000	0.000	
43.75	45.14	0.042	0.045	0.393	0.0117	3.80	45.18	45.40	0.419	4.00	-15.039	0.430	0.027	0.080	0.000	0.000	
45.07	45.03	0.042	0.045	0.393	0.0117	3.80	45.08	45.30	0.419	4.00	-15.038	0.430	0.027	0.080	0.000	0.000	
46.39	44.93	0.042	0.045	0.393	0.0117	3.80	44.97	45.19	0.419	4.00	-15.038	0.430	0.027	0.080	0.000	0.000	
47.70	44.82	0.042	0.045	0.393	0.0117	3.80	44.86	45.09	0.419	4.00	-15.038	0.430	0.027	0.080	0.000	0.000	
49.02	44.72	0.042	0.045	0.393	0.0117	3.80	44.76	44.98	0.419	4.00	-15.038	0.430	0.027	0.080	0.000	0.000	
50.34	44.61	0.042	0.045	0.393	0.0117	3.80	44.65	44.88	0.419	4.00	-15.038	0.430	0.027	0.080	0.000	0.000	
51.66	44.51	0.042	0.045	0.393	0.0117	3.80	44.55	44.77	0.419	4.00	-15.038	0.430	0.027	0.080	0.000	0.000	